

Factor:

$$x^2 + 8x + 16$$

x^2	$4x$
$4x$	16

$$(x+4)(x+4)$$

$$(x+4)^2$$

ax^2	
	c

split
bx

Factors ac
Add b

$$ax^2 + bx + c$$

$$x^2 - 10x + 25$$

x^2	$-5x$
$-5x$	25

$$(x-5)(x-5)$$

$$(x-5)^2$$

Equation of a Circle

Solving by completing the square:

$$x^2 - 8x = -16$$

$$\begin{array}{c} \downarrow \div 2 \\ (-4)^2 \end{array}$$

$$x^2 - 8x + 16 = -16 + 16$$

$$\sqrt{(x-4)^2} = \sqrt{0}$$

$$\begin{array}{c} x-4 = 0 \\ +4 \quad +4 \\ x = 4 \end{array}$$

$$x^2 - 10x + \quad = \quad -9$$

$$\begin{array}{c} \downarrow \div 2 \\ (-5)^2 \end{array}$$

$$x^2 - 10x + 25 = -9 + 25$$

$$\sqrt{(x-5)^2} = \sqrt{16}$$

$$\begin{array}{c} x-5 = 4, \quad -4 \\ +5 \quad +5 \quad +5 \end{array}$$

$$x = 9, 1$$

Equation of a Circle: The equation of a circle is represented as $(x-h)^2+(y-k)^2=r^2$ where (h,k) is the center and r is the radius.



Point
on
circle

Write an equation of a circle with the center (5, 4) and radius 7.

$$(x-h)^2 + (y-k)^2 = r^2$$

$$(x-5)^2 + (y-4)^2 = 49$$

$$(x+6)^2 + (y-2)^2 = 25$$

Center: (-6, 2) radius: 5

The equation $x^2 - 4x + y^2 + 2y = 20$ defines a circle. What are the coordinates of the center and the radius?

$$(x-h)^2 + (y-k)^2 = r^2$$

$$x^2 - 4x + 4$$

$$\downarrow$$

$$(-2)^2$$

$$(x-2)^2$$

$$y^2 + 2y + 1 = 20 + 4 + 1$$

$$\downarrow$$

$$(1)^2$$

$$(y+1)^2$$

$$(x-2)^2 + (y+1)^2 = 25$$

center: (2, -1) Radius: 5

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